

LIMIT STATE METHOD

PART-II

DEPT. OF TECHNICAL EDUCATION U.P.
GOVT. POLYTECHNIC SHAHJAHANPUR

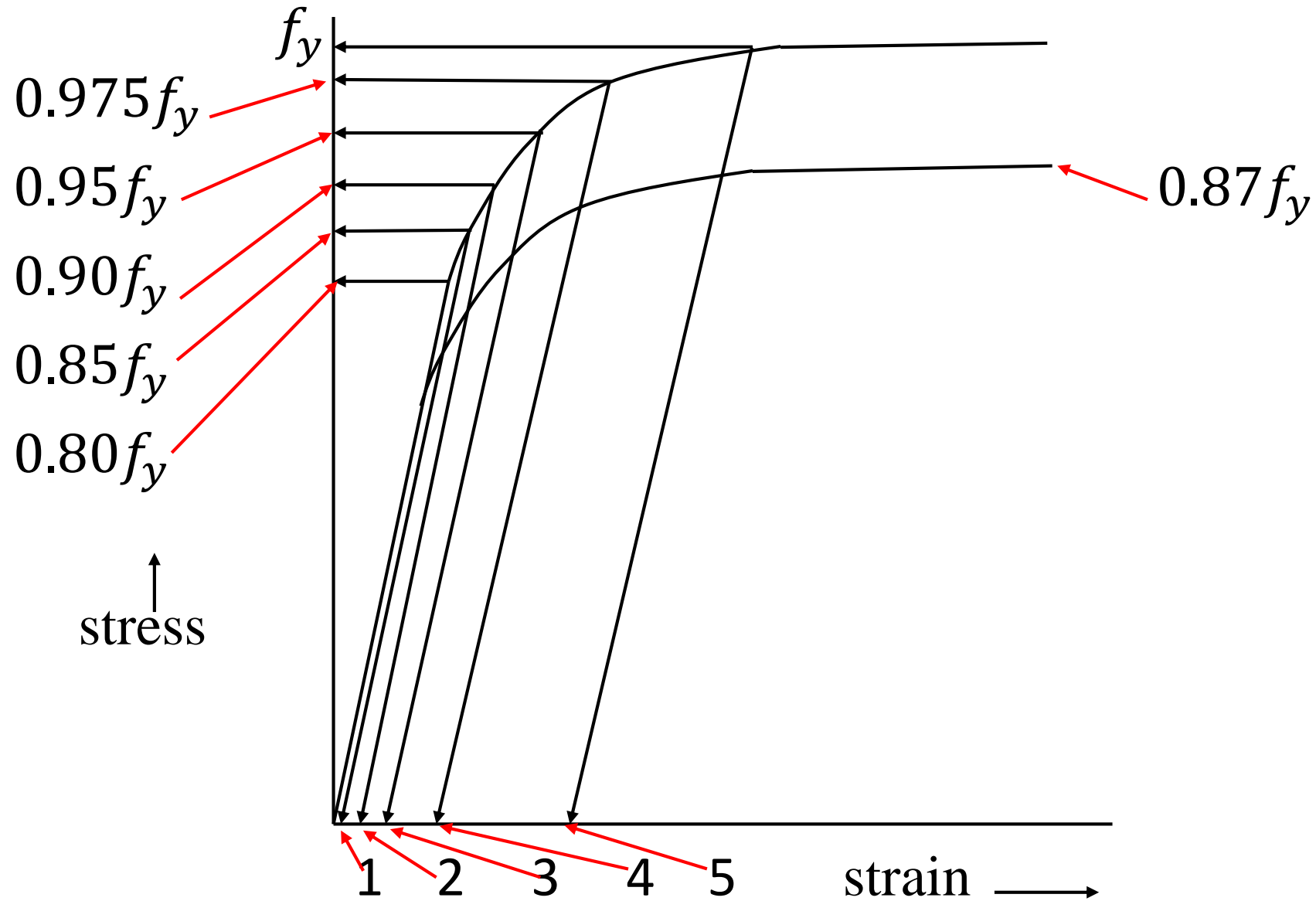
PRESENTED BY

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IDEAL CURVE FOR Fe 415 / Fe500 STEEL



STRESS IN STEEL GRADE Fe415

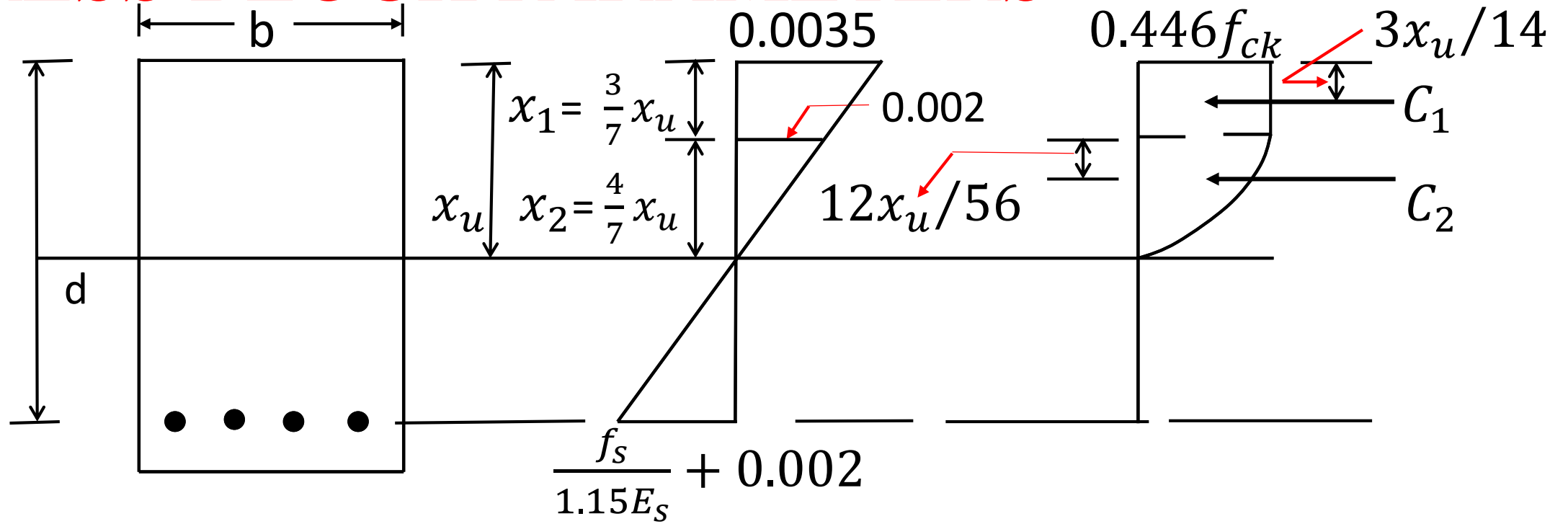
S.NO	STRESS N/mm^2	ELASTIC STRAIN $e = \frac{f_s}{E}$ $E = 2 * 10^5$	INELASTIC STRAIN	TOTAL STRAIN
1	$0.80 * 0.87 * 415 = 288.4$	0.00144	0.00	0.00144
2	$0.85 * 0.87 * 415 = 306.89$	0.00153	0.0001	0.00163
3	$0.90 * 0.87 * 415 = 324.95$	0.00162	0,0003	0.00192
4	$0.95 * 0.87 * 415 = 343.00$	0.00171	0.0007	0.00241
5	$0.975 * 0.87 * 415 = 352.00$	0.00176	0.001	0.00276
6	$0.87 * 415 = 361.05$	0.00180	0.002	0.0038

ASSUMPTIONS

- Plane section before bending remains plane after bending
- Maximum strain in outermost fiber of concrete is 0.0035
- Stress diagram can be of any shape
- Tensile strength of concrete is ignored
- Stress in steel can be determined from stress strain curve
- Maximum strain in steel at failure must be greater than or equal to

$$e_{s \max} \geq \frac{0.87 f_y}{E_s} + 0.002$$

STRESS BLOCK PARAMETERS



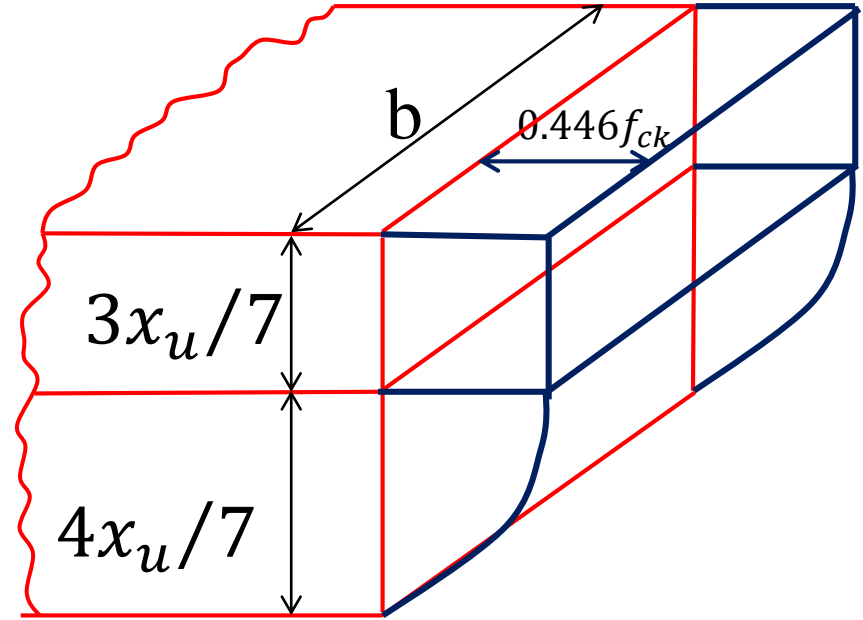
Let x_u be the depth of neutral axis from the top fiber

$$\frac{x_2}{x_u} = \frac{0.002}{0.0035}$$

$$\therefore x_2 = \frac{4}{7} x_u$$

- $$x_1 = x_u - x_2$$

$$x_1 = \frac{3}{7} x_u$$



Compressive force = area * stress

Compressive force $C_1 = \frac{3}{7} x_u \times b \times 0.446 f_{ck}$
 $= 0.19 f_{ck} b x_u$

Compressive force $C_2 = \frac{2}{3} \times \frac{4}{7} x_u \times b \times 0.446 f_{ck}$
 $= 0.17 f_{ck} b x_u$

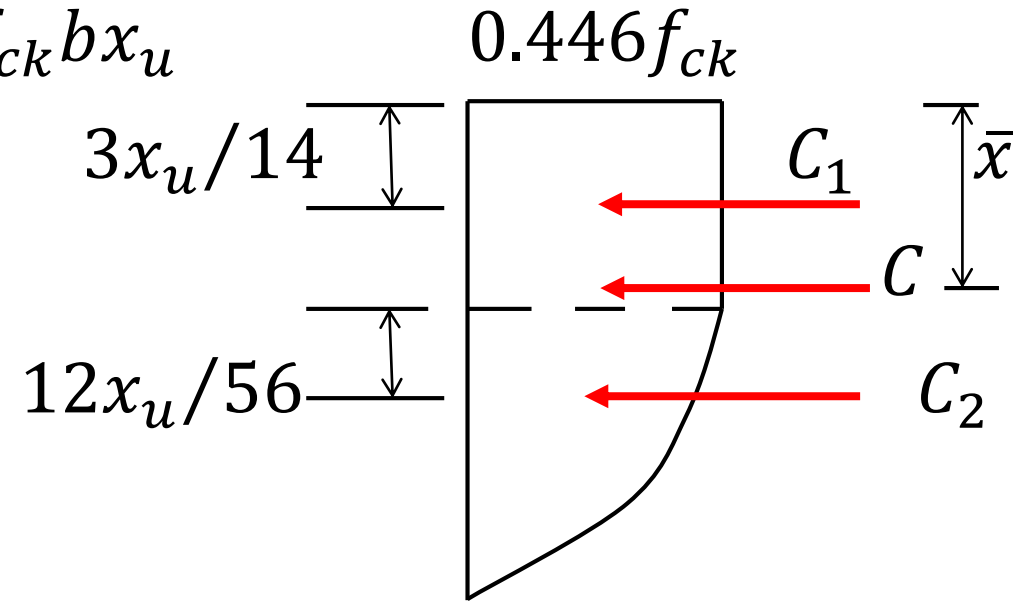
Total force

$$C = C_1 + C_2$$

$$C = 0.36f_{ck}bx_u$$

to find point of action of C

taking moment of forces about top edge

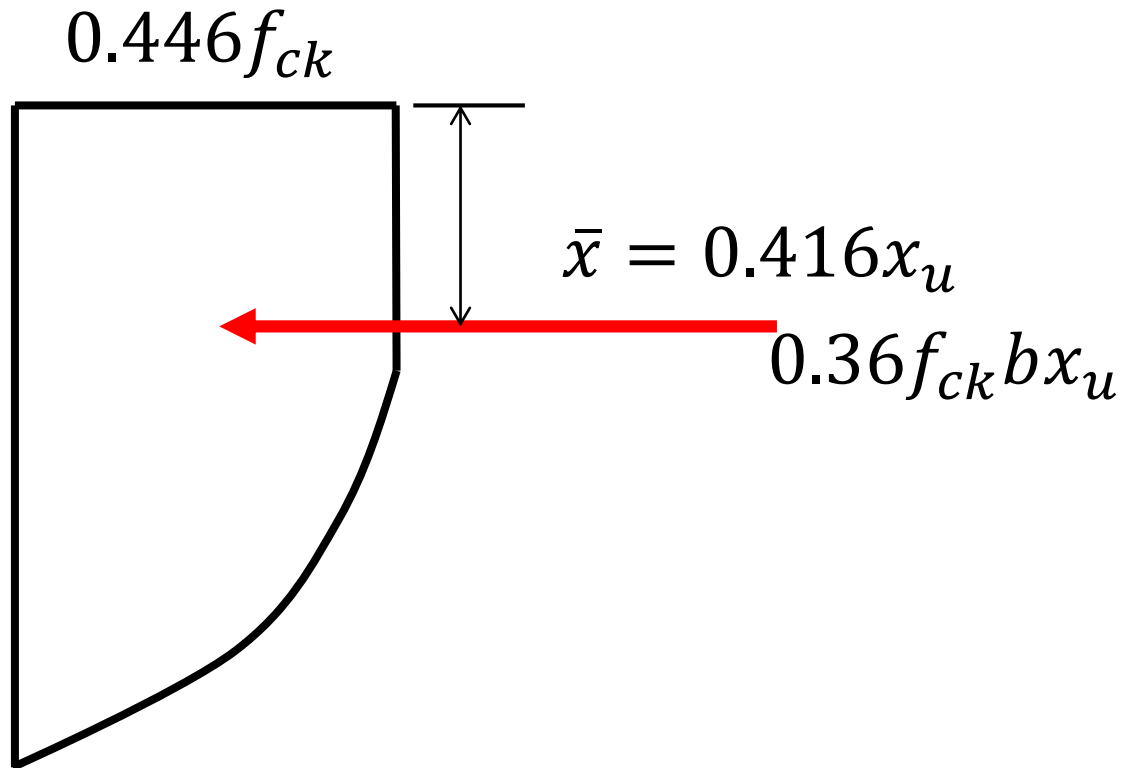


$$C \times \bar{x} = C_1 \times \frac{3}{14}x_u + C_2 \times \left(\frac{3}{7}x_u + \frac{12}{56}x_u \right)$$

$$0.36f_{ck}bx_u \times \bar{x} = 0.19f_{ck}bx_u \times \frac{3}{14}x_u + 0.17f_{ck}bx_u \times \left(\frac{3}{7}x_u + \frac{12}{56}x_u\right)$$

$$\therefore \bar{x} = 0.416x_u$$

Stress block parameters are shown below



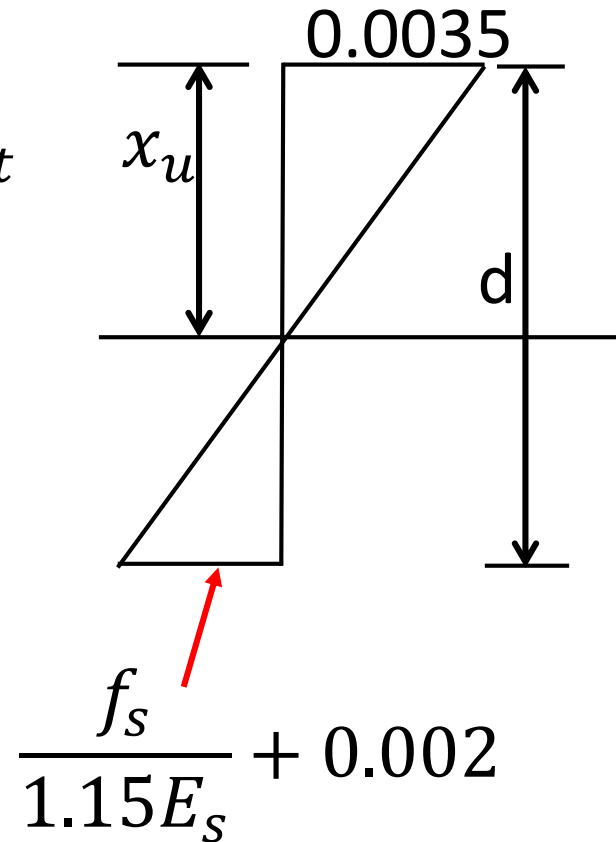
NEUTRAL AXIS

- Equivalent area is used to find neutral axis in working stress method
- In limit state compressive and tensile forces are equated

$$C = T$$

$$0.36f_{ck}bx_u = 0.87f_y \times A_{st}$$

$$x_u = \frac{0.87f_y A_{st}}{0.36f_{ck}bx_u}$$



➤ Depth of neutral axis for balanced section

$$\frac{x_u \text{ lim}}{d - x_u \text{ lim}} = \frac{0.0035}{\frac{f_y}{1.15E_s} + 0.002}$$

Putting $E_s = 2 \times 10^5 \text{ N/mm}^2$

$$x_u \text{ lim} = \frac{700 d}{1100 + 0.87f_y}$$

$$f_y = 250 \text{ N/mm}^2, x_u \text{ lim} = 0.53d$$

$$f_y = 415 \text{ N/mm}^2, x_u \text{ lim} = 0.48d$$

$$f_y = 500 \text{ N/mm}^2, x_u \text{ lim} = 0.46d$$

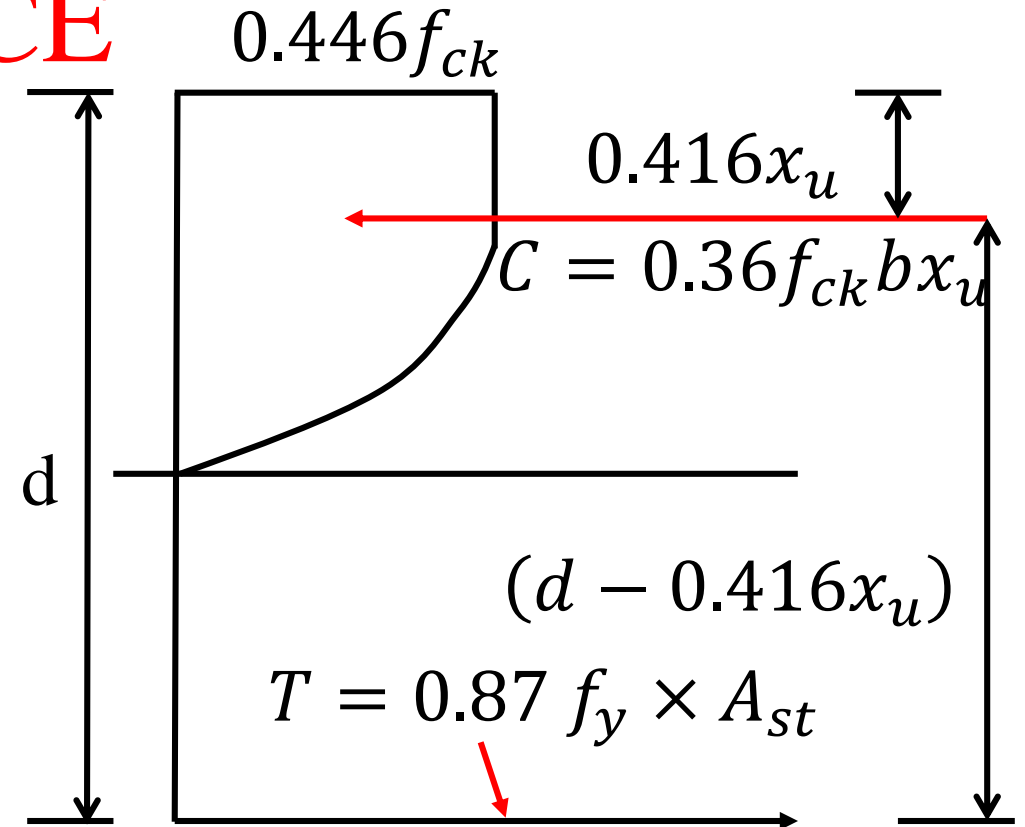
MOMENT OF RESISTANCE

MR = compressive force * lever arm
= tensile force * lever arm

$$MR = 0.36 f_{ck} b x_u (d - 0.416 x_u)$$

$$MR = 0.87 f_y \times A_{st} (d - 0.416 x_u)$$

where $x_u \leq x_{u \text{ lim}}$



THANK YOU